Topic 5

Rhythm Analysis (some slides are adapted from Zafar Rafii and some figures are from Meinard Mueller)

Definitions for Rhythm Analysis

• **Rhythm:** "movement marked by the regulated succession of strong and weak elements, or of opposite or different conditions."

---- Oxford English Dictionary

- **Beat:** basic unit of time in music
- **Tempo:** speed or pace of a given piece, typically measured in beats per minute (BPM)





More Definitions

- **Onset**: single instant marking the beginning of transient
 - Onsets often occur on beats.
- Attack: sharp increase of energy
- **Transient**: a short duration with high amplitude within which signal evolves quickly



More Definitions

• Measure (or bar): segment of time defined by a given number of beats



A 4-beat measure drum pattern. [http://en.wikipedia.org/wiki/Metre (music)]

More Definitions

• **Meter:** Organization of music into regularly recurring measures of stressed and unstressed beats



Hypermeter: 4-beat measure and 4-measure hypermeasure. Hyperbeats in red. [http://en.wikipedia.org/wiki/Metre (music)]

Rhythm Analysis Tasks

- Onset Detection
- Beat Tracking
- Tempo Estimation
- Higher-level Structure Analysis



Why is it important?

- Intellectual merit
 - Important component of music understanding
 - Music cognition research

- Broad applications
 - Identify/classify/retrieve by rhythmic similarity
 - Music segmentation/summarization
 - Audio/video synchronization
 - Source separation

Onset Detection

- Signal processing: define a detection function
 - Energy-based
 - Spectral-based
 - Phase-based
- Machine Learning: learn patterns from labeled data
 - Probabilistic models
 - Neural networks



Energy-based Onset Detection



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Energy-based Onset Detection

- Pros and Cons
 - Simple
 - Works well for percussive sounds
 - Soft onsets by string/wind instruments are hard to detect
 - Tremolo/vibrato can cause false detections
- How to improve
 - Use logarithmic-energy to replace linear energy
 - Perform analysis in different frequency bands, then summarize

Spectral-based Onset Detection

- STFT to get magnitude spectrogram $|\chi|$
- (optional) compression

 $\mathcal{Y} := \Gamma_{\gamma}(|\mathcal{X}|) = \log(1 + \gamma \cdot |\mathcal{X}|)$

- Spectral flux:
 - Take derivative w.r.t. time (half-wave rectified)

$$\Delta_{\text{Spectral}}(n) := \sum_{k=0}^{K} |\mathcal{Y}(n+1,k) - \mathcal{Y}(n,k)|_{\geq 0}$$



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Spectral-based Onset Detection

- Pros and Cons
 - More complex than energy-based
 - Can weigh different frequencies differently
 - Works better for soft onsets (e.g., legato notes) and polyphonic music
 - Still doesn't work very well for vibrato

Tempo Estimation

- Tempo = beats / minutes
- Beat tracking is a sufficient but not a necessary condition for tempo estimation
- How to estimate tempo without tracking beats?
- Idea: look at the regularity of onsets
- Assumptions
 - Onsets mostly occur on beats
 - Tempo is constant within a period of time

Tempo Estimation



- Take the onset strength curve and analyze its periodicity
 - Autocorrelation
 - STFT



Beat Tracking

- Identify the beat times, i.e., the times to which we tap our feet
 - Detected onsets provide useful but noisy information, since not all onsets are on beats.
 - Estimated tempo tells us the space between two beats, but not the exact locations (i.e., phase).
- How to identify beats?
- To simply the problem, we assume
 - Onsets, especially strong ones, are mostly on beats.
 - Tempo is constant.

Beat Tracking

- A 2-step approach
 - Step 1: Tempo estimation
 - Step 2: Identify beats from onsets using the tempo
 - Create an impulse train (i.e., "comb") with the tempo
 - Cross-correlate the "comb" with the onset strength curve.
 - The lag that gives us the highest cross-correlation value tells us the beat phase.

• A 2-step approach, illustration



• Problem: too rigid about beat spacing

- Beat tracking: finding a sequence of beat locations such that they [Ellis, 2007]
 - 1) are well aligned with strong onsets
 - 2) mostly regularly spaced



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Rough

- Suppose beat locations are precise to audio frames, and suppose there are *N* frames, then how many possible sequences?
 - 2^{N} (although many are bad ones!)
 - Can't enumerate all!

• Key idea: reuse calculations by recursion!

- Consider a beat sequence $B_n = (b_1, b_2, \dots, b_L)$ where $b_L = n$.
- Let *D*(*n*) be the maximal score among all sequences that end at *n*, with various lengths.
- Assume B_n is the optimal sequence
- Then if L = 1 $\mathbf{D}(n) = \Delta(n)$ recursion if L > 1 $\mathbf{D}(n) = \Delta(n) + \lambda P_{\hat{\delta}}(n - b_{L-1}) + \mathbf{D}(b_{L-1})$

• Considering the two cases, we have

$$\mathbf{D}(n) = \Delta(n) + \max \begin{cases} 0, \\ \max_{m \in [1:n-1]} \left\{ \mathbf{D}(m) + \lambda P_{\hat{\delta}}(n-m) \right\} \end{cases}$$

- We can calculate D(n) from $D(1) = \Delta(1)$.
- Record the preceding beat

$$\mathbf{P}(n) := \underset{m \in [1:n-1]}{\operatorname{argmax}} \left\{ \mathbf{D}(m) + \lambda P_{\hat{\delta}}(n-m) \right\}$$

- Best score $\mathbf{S}(B^*) = \max_{n \in [0:N]} \mathbf{D}(n)$
- Trace back from $b_L = n^*$ is best sequence

Rhythmic Structure



- One approach: detect onsets; analyze tempo and beats at different levels.
- Another approach: analyze repetition of spectral content
 - Beat spectrum

- Definition
 - Using the autocorrelation function, we can derive the beat spectrum [Foote et al., 2001]



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• Use

 The beat spectrum reveals the hierarchically periodically repeating structure of the audio



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- Calculation
 - Compute the power spectrogram from the audio using the STFT (square of magnitude spectrogram)



- Calculation
 - Compute the autocorrelation of the rows of the spectrogram



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- Calculation
 - Compute the mean of the autocorrelations (of the rows)



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State-of-the-Art

- Some interesting links
 - Dannenberg's articles on beat tracking: <u>http://www.cs.cmu.edu/~rbd/bib-beattrack.html</u>
 - Goto's work on beat tracking: <u>http://staff.aist.go.jp/m.goto/PROJ/bts.html</u>
 - Ellis' Matlab codes for tempo estimation and beat tracking: <u>http://labrosa.ee.columbia.edu/projects/beattrack/</u>
 - Heydari's BeatNet and SingNet: https://github.com/mjhydri/BeatNet

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